

The PHY 357: Intermediate Physics Lab final projects presentation

First experiments from the SUNY Cortland wind tunnel

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Cody Wagner

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and Dr. Eric Edlund
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May 7, 2021

Outline of the presentation

- History of the wind tunnel
- Brief overview of fluid dynamics theory
- Project 1: characterization of the wind tunnel
- Project 2: drag forces on sports balls
- Project 3: drag forces on vehicles
- Project 4: lift forces on wings
- Conclusions and outlook

Wind tunnels in many sizes, shapes, and speeds

Large & full-scale wind tunnels

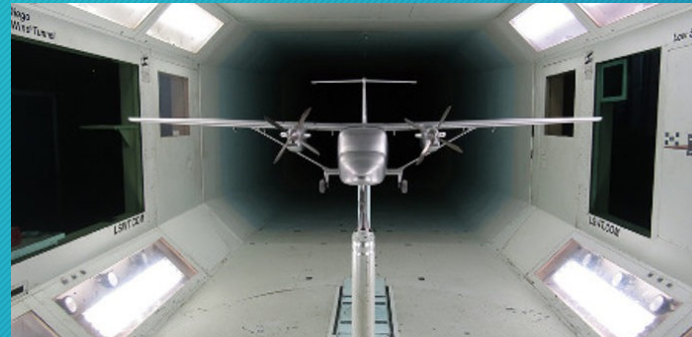


NFAC (US Air Force)



16S (US Air Force)

Medium-scale wind tunnels (usually recirculating)



Textron Aviation



Ferrari

Small-scale wind tunnels (usually open)



Tec Equipment, Inc.



Original Wright brothers wind tunnel

History of the SUNY Cortland wind tunnel

January: construction begins



February: construction complete



March: faculty development grant to purchase measurement equipment



April: first measurements



May 7: first presentation of experiments

Windy ENvironment Developer (WEN-D)



Velocity measurements: Pitot tube

Lift and drag measurements: 2-axis force balance

Theory part 1: the force law

Navier-Stokes equation:

$$\rho \frac{d}{dt} \vec{v} = -\vec{\nabla} p + \mu \nabla^2 \vec{v} + \sum \vec{F}_{ext}$$

response

internal forces

external forces

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internal forces

external forces

A special case of Newton's 2nd law:

$$m \frac{d}{dt} \vec{v} = \sum \vec{F}$$

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response

internal forces

external forces

A special case of Newton's 2nd law:

$$m \frac{d}{dt} \vec{v} = \sum \vec{F}$$

In dimensionless form:

$$\frac{d}{dt} \vec{v} = -\frac{1}{M^2} \vec{\nabla} p + \frac{1}{Re} \nabla^2 \vec{v} + \dots$$

Mach number: $M = \frac{v}{v_{th}} \sim \frac{\text{inertial motion}}{\text{thermal motion}}$

Reynolds number: $Re = \frac{\rho v L}{\mu} \sim \frac{\text{inertial force}}{\text{viscous force}}$

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$$\frac{d}{dt} \vec{v} = -\frac{1}{M^2} \vec{\nabla} p + \frac{1}{Re} \nabla^2 \vec{v} + \dots$$

Mach number:

(experiment < 0.05)
(can treat air as uniform)

$$M = \frac{v}{v_{th}} \sim \frac{\text{inertial motion}}{\text{thermal motion}}$$

Reynolds number:

(experiment: $10^4 - 10^5$)
(car @ 60 mph ~ 3×10^6)

$$Re = \frac{\rho v L}{\mu} \sim \frac{\text{inertial force}}{\text{viscous force}}$$

Theory part 2: conservation laws

The Bernoulli equation:
(conservation of energy)

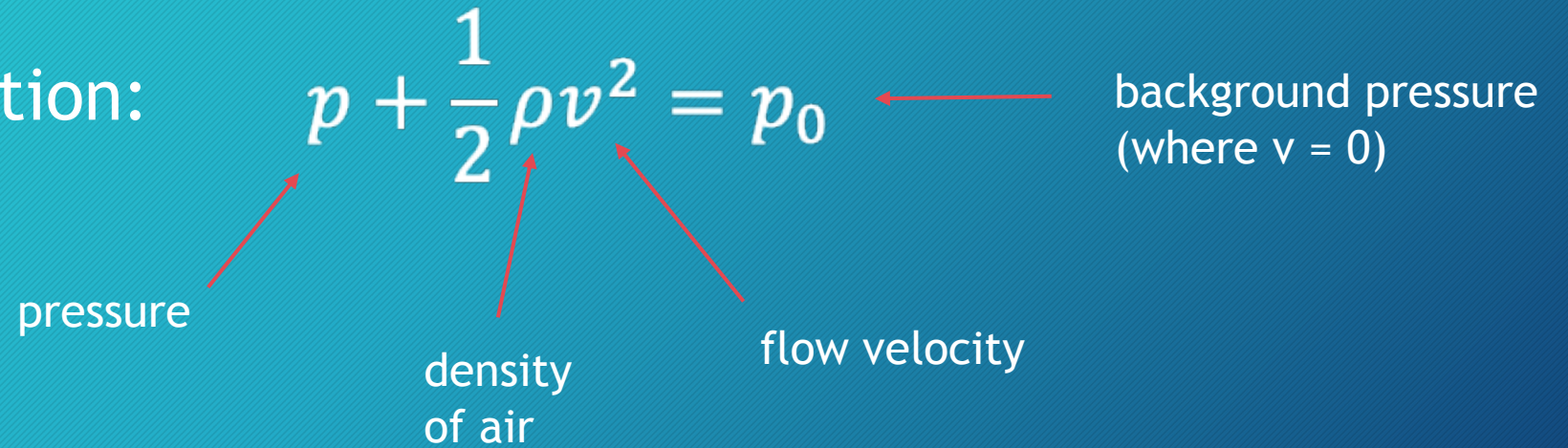
$$p + \frac{1}{2} \rho v^2 = p_0$$

pressure

density of air

flow velocity

background pressure
(where $v = 0$)

The diagram shows the Bernoulli equation $p + \frac{1}{2} \rho v^2 = p_0$ centered on the page. Four red arrows point from text labels to the corresponding terms in the equation: 'pressure' points to p , 'density of air' points to ρ , 'flow velocity' points to v , and 'background pressure (where v = 0)' points to p_0 .

Theory part 2: conservation laws

The Bernoulli equation:
(conservation of energy)

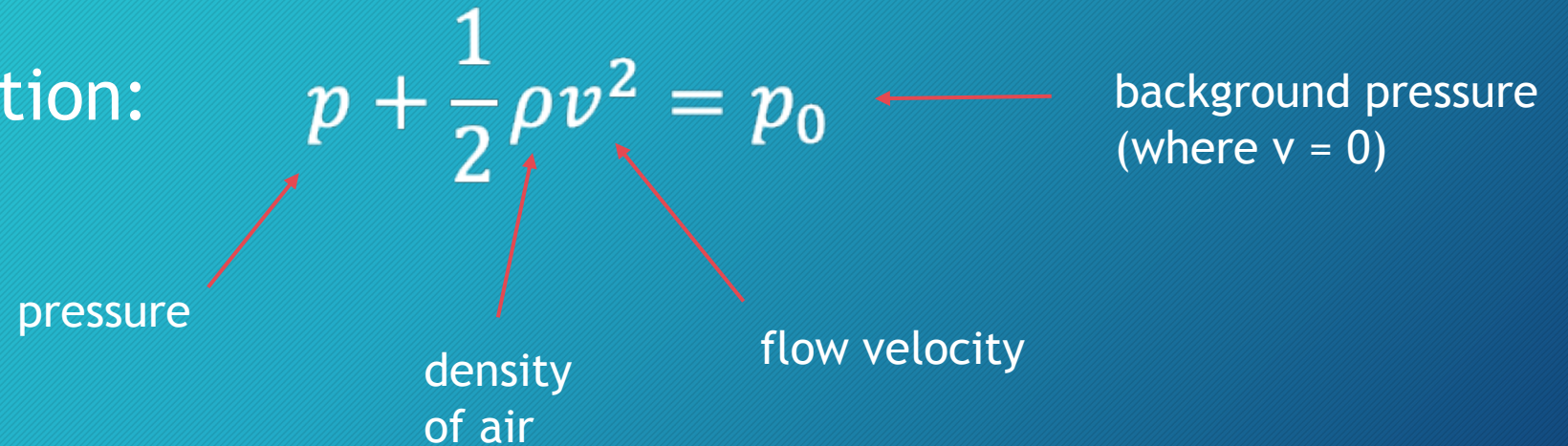
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pressure

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The diagram shows the Bernoulli equation $p + \frac{1}{2} \rho v^2 = p_0$. Red arrows point from the labels 'pressure', 'density of air', and 'flow velocity' to the terms p , ρ , and v respectively. Another red arrow points from the label 'background pressure (where v = 0)' to the term p_0 .

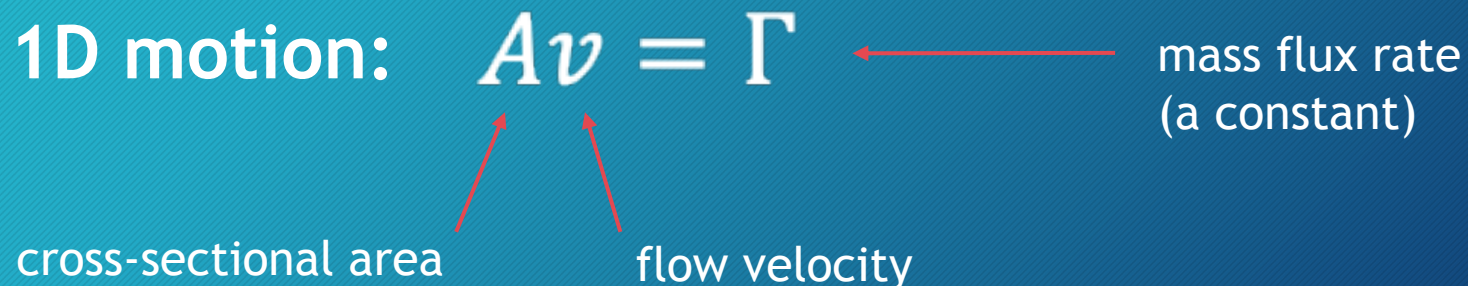
Conservation of mass for
systems with 1D motion:

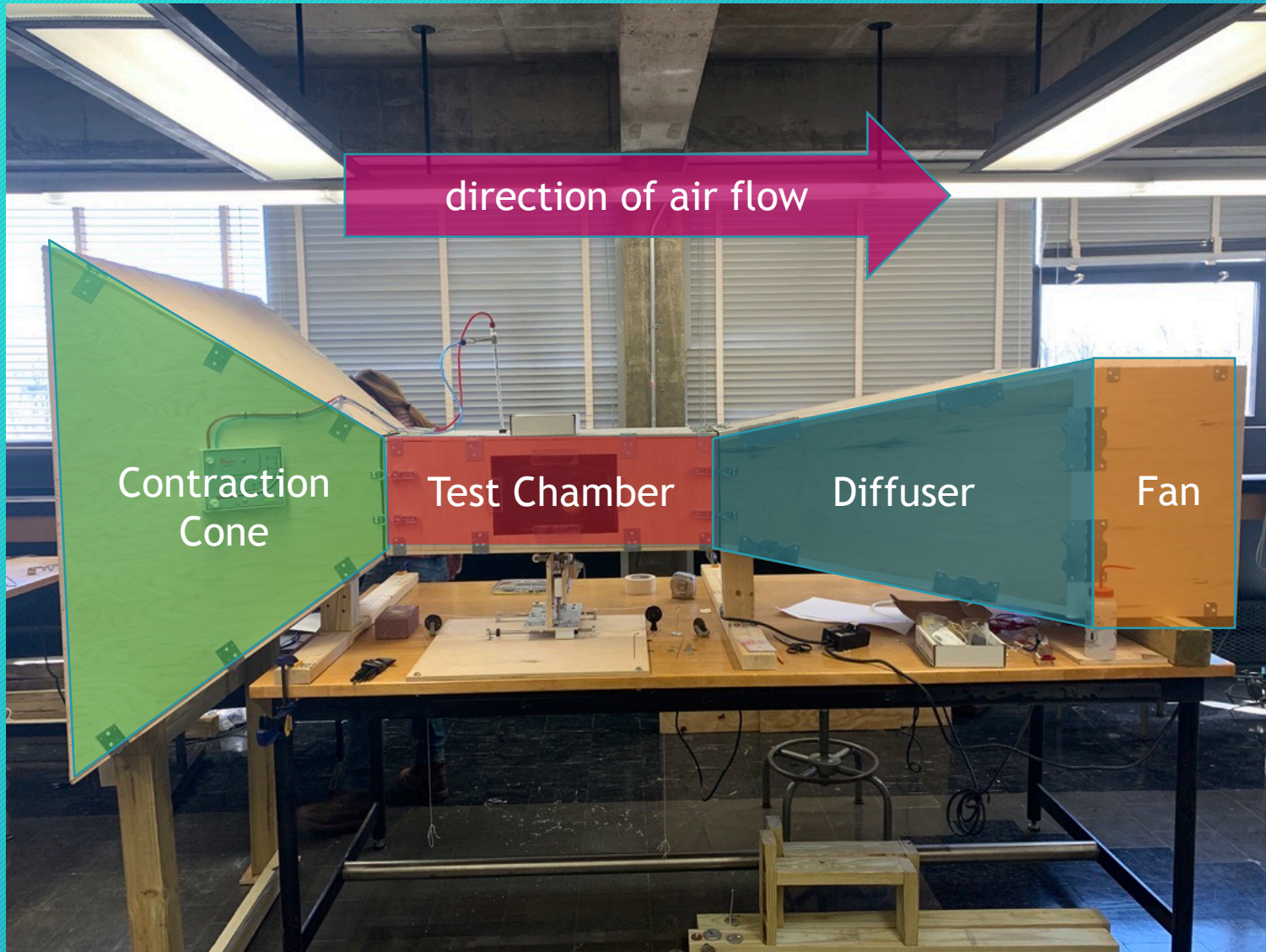
$$Av = \Gamma$$

cross-sectional area

flow velocity

mass flux rate
(a constant)

The diagram shows the mass conservation equation $Av = \Gamma$. Red arrows point from the labels 'cross-sectional area' and 'flow velocity' to the terms A and v respectively. Another red arrow points from the label 'mass flux rate (a constant)' to the term Γ .



direction of air flow

Contraction
Cone

Test Chamber

Diffuser

Fan

Contraction Cone

High Pressure

Low Velocity

Test Chamber

High Velocity

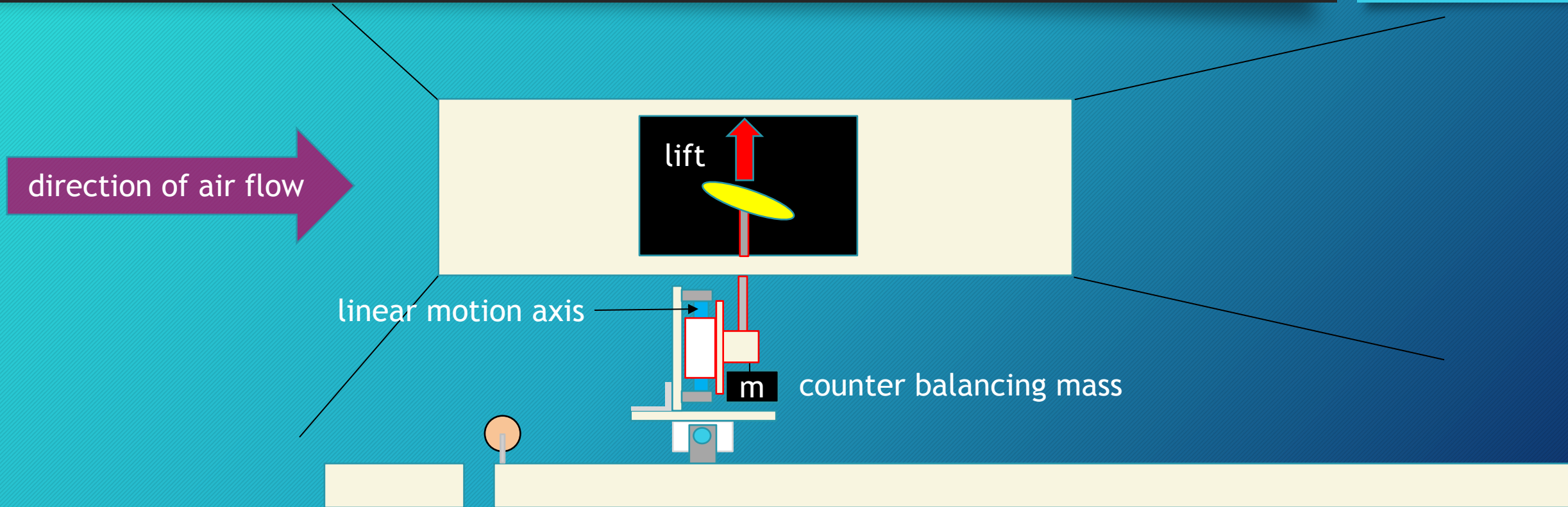
Low Pressure

Diffuser

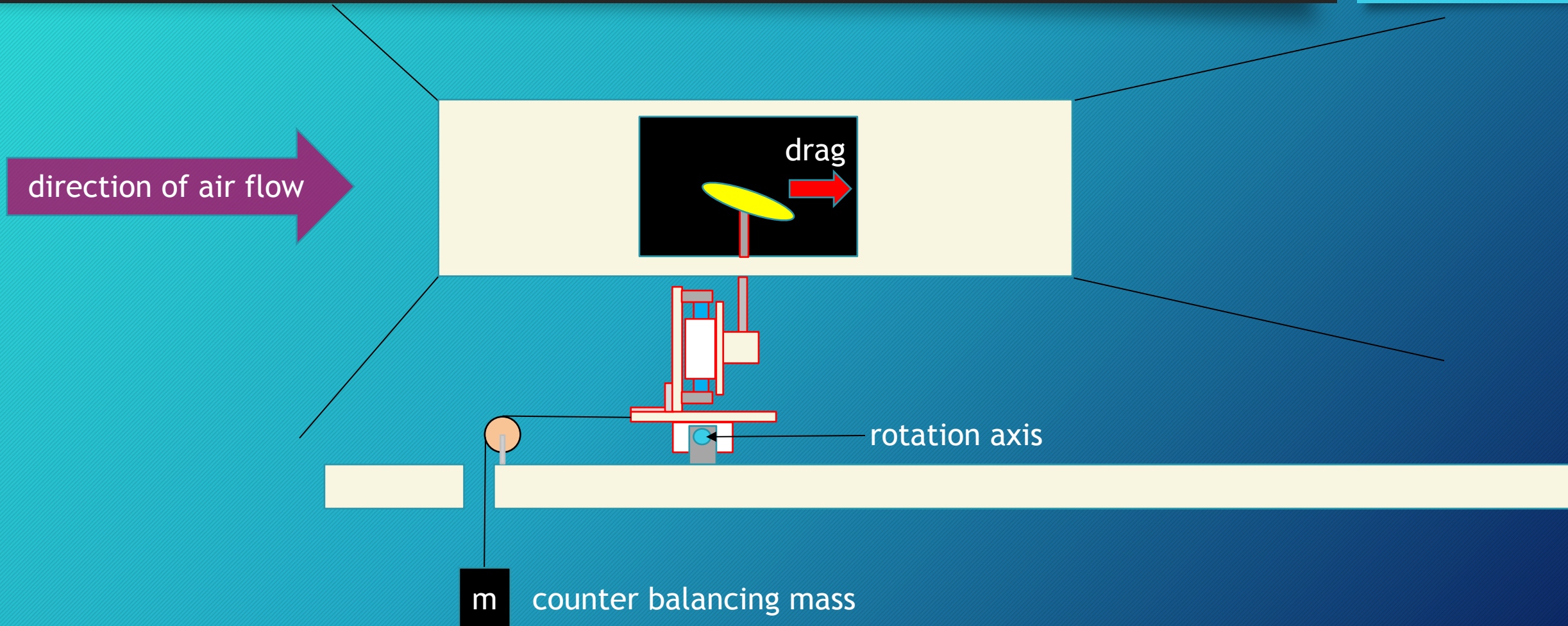
High Pressure

Low Velocity

The force balance: measuring LIFT forces



The force balance: measuring DRAG forces



Project 1: Wind tunnel characterization

Chelsea Allain, Greg Cassiano, Victoria Kilfeather

- How can a Pitot tube be used to calculate for velocity in a wind tunnel?
- What are the differences in velocity throughout the wind tunnel?

Two methods for measuring wind speed

Method 1: the anemometer



Method 2: the Pitot tube

Measure pressure at two locations

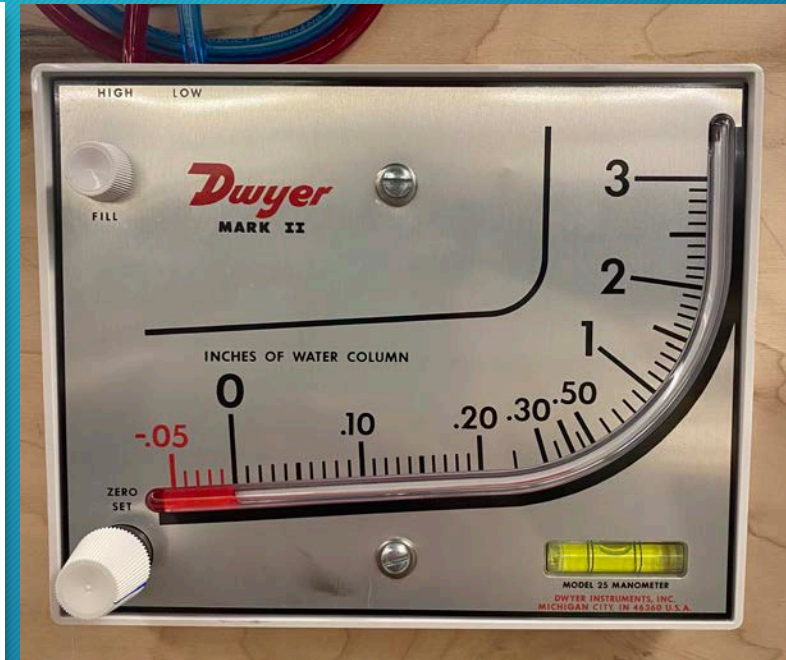
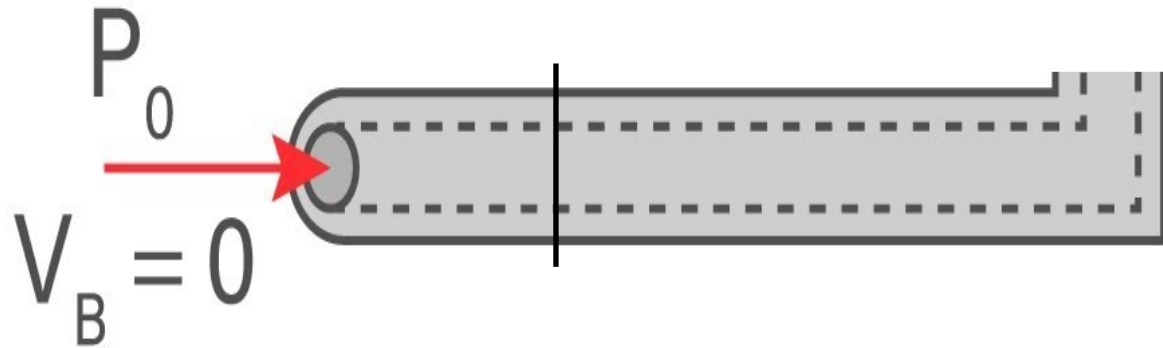
Rearrange the Bernoulli equation to solve for velocity:

$$v = \sqrt{\frac{2 \Delta p}{\rho}}$$

Δp = Stagnation Pressure - Static Pressure



PITOT TUBE EXPERIMENT



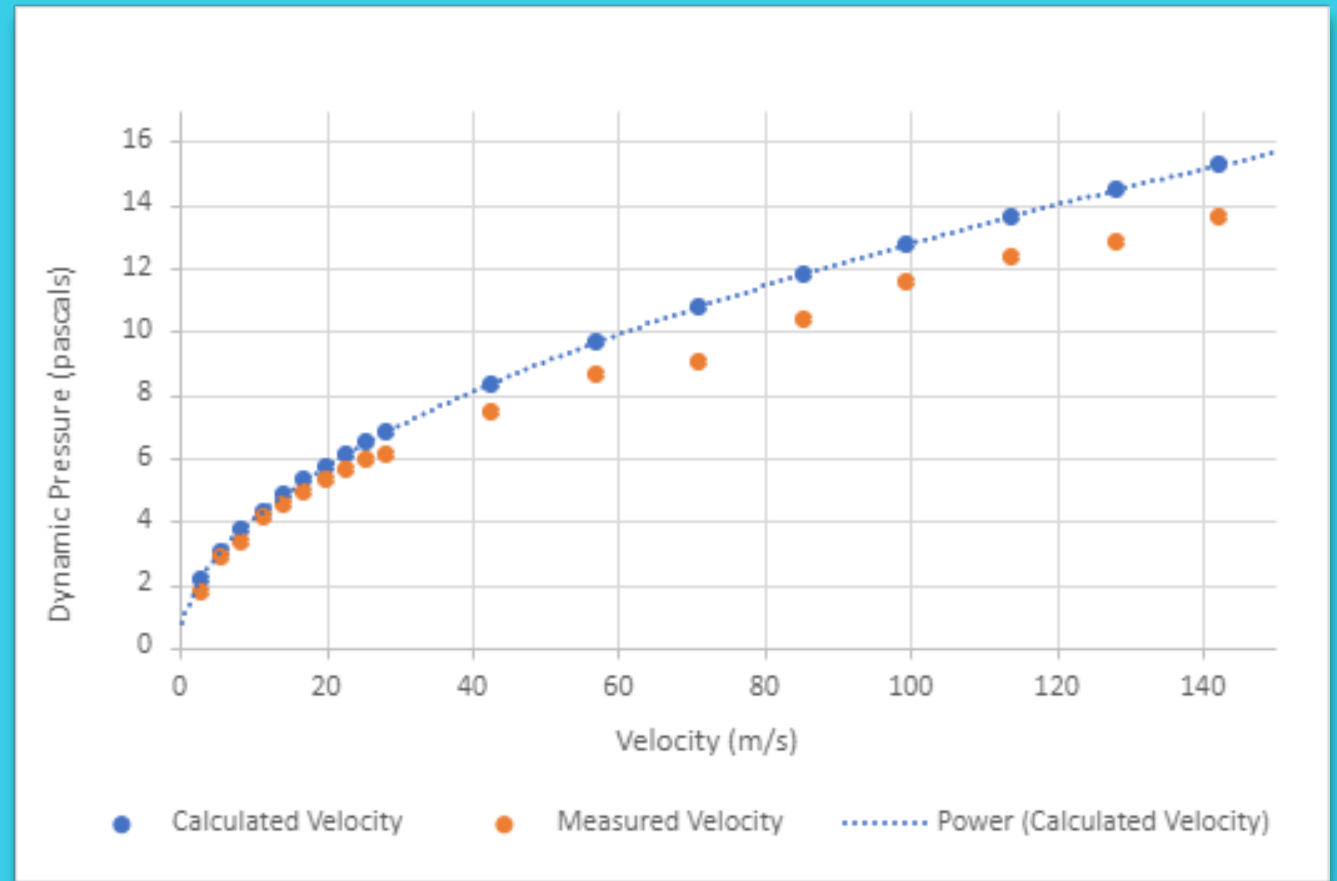
Pressure gauge uses units of inches of water

Conversion equation is $V \text{ m/s} = \sqrt{\frac{2(\Delta P * 284.84)}{1.225 \text{ kg/m}^3}}$ or $V \text{ m/s} = 21.56\sqrt{\Delta P}$.

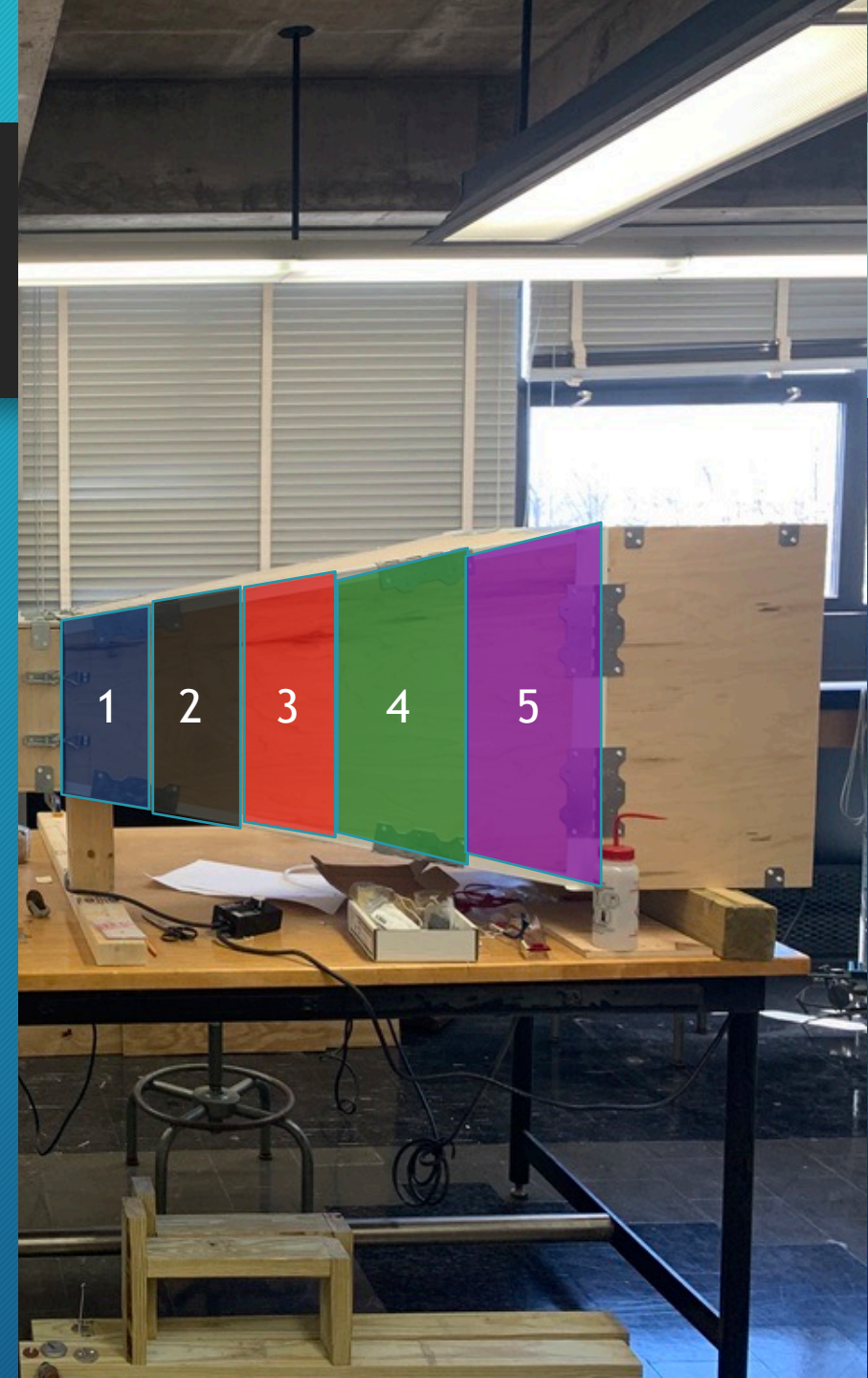
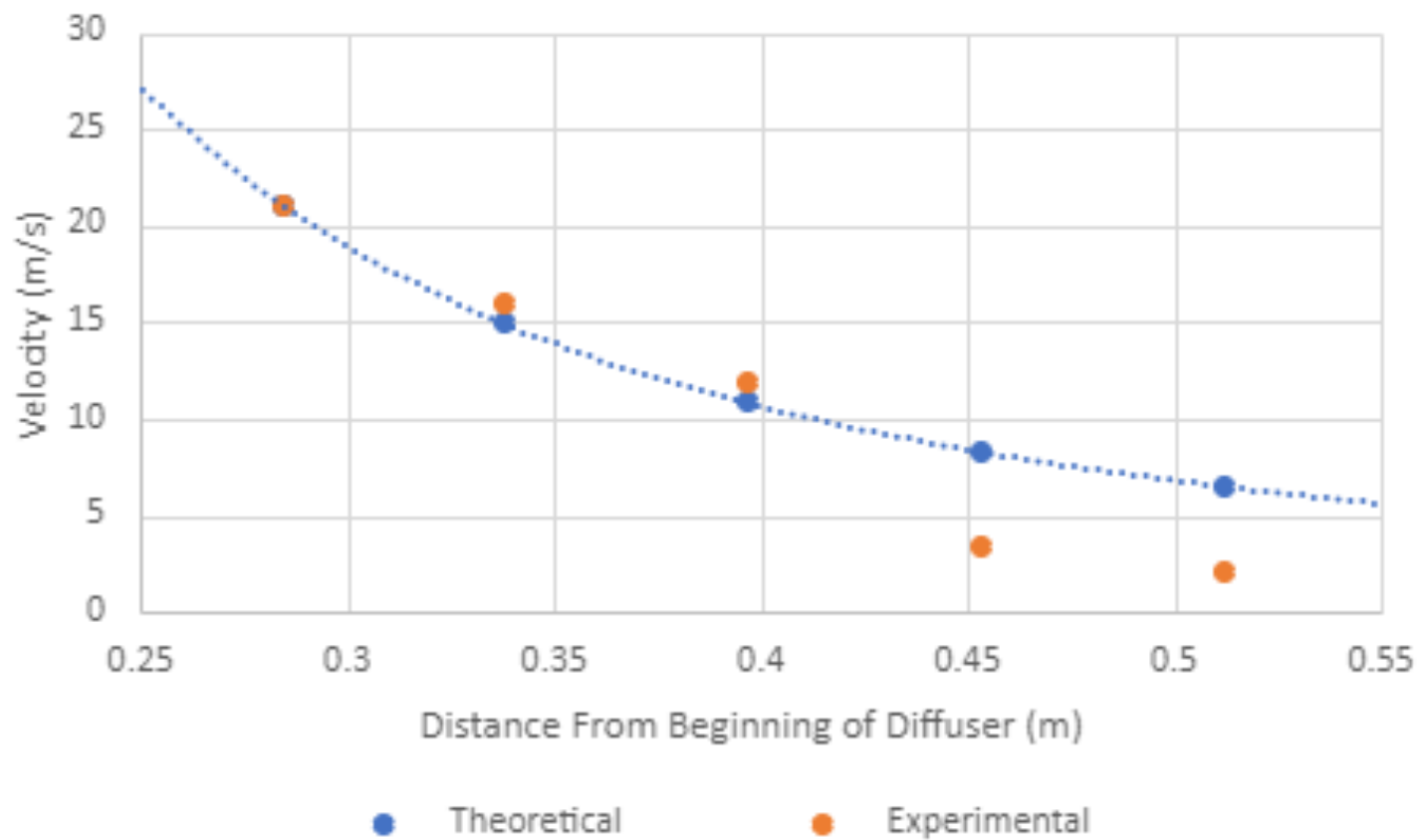
Pitot
Tube

Comparing Pitot tube and anemometer data

- All measurements shown on this graph were taken in the testing chamber
- The pitot tube and the anemometer were in the middle of the testing chamber.



Velocity variation in the diffuser



Project 2: Measuring drag coefficients of sports balls

Jose Diaz Duran, Avery Tompkins, Dakota (Cody) Wagner

- How much does the surface texture of a sphere impact the force of drag?
- Using the wind tunnel, we measured the drag of spheres of different surface texture
- Measured the drag forces on a lacrosse, tennis, blitz, and baseball
- Balanced at zero wind speed, then increased the speed to measure the force of drag on each sphere

Theoretical model of turbulent drag

Drag force: $F_{drag} = \frac{1}{2} \rho v^2 C_d A$

Solving for the drag coefficient:

$$C_d = \frac{2 F_{drag}}{\rho_{air} v^2 A}$$

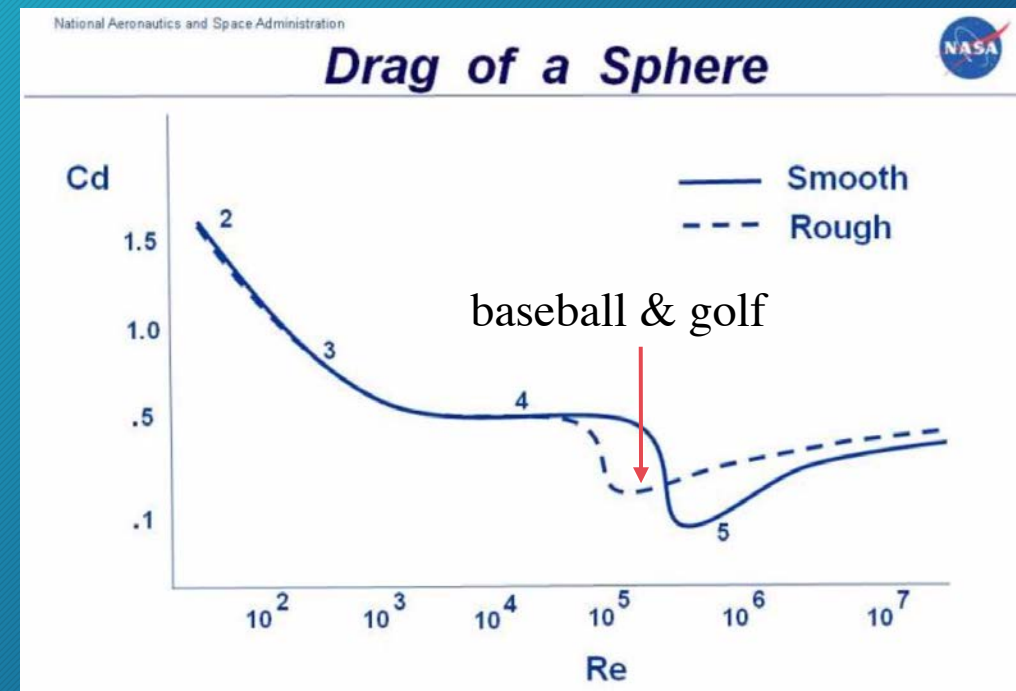
Where:

ρ = density of air

v = wind speed

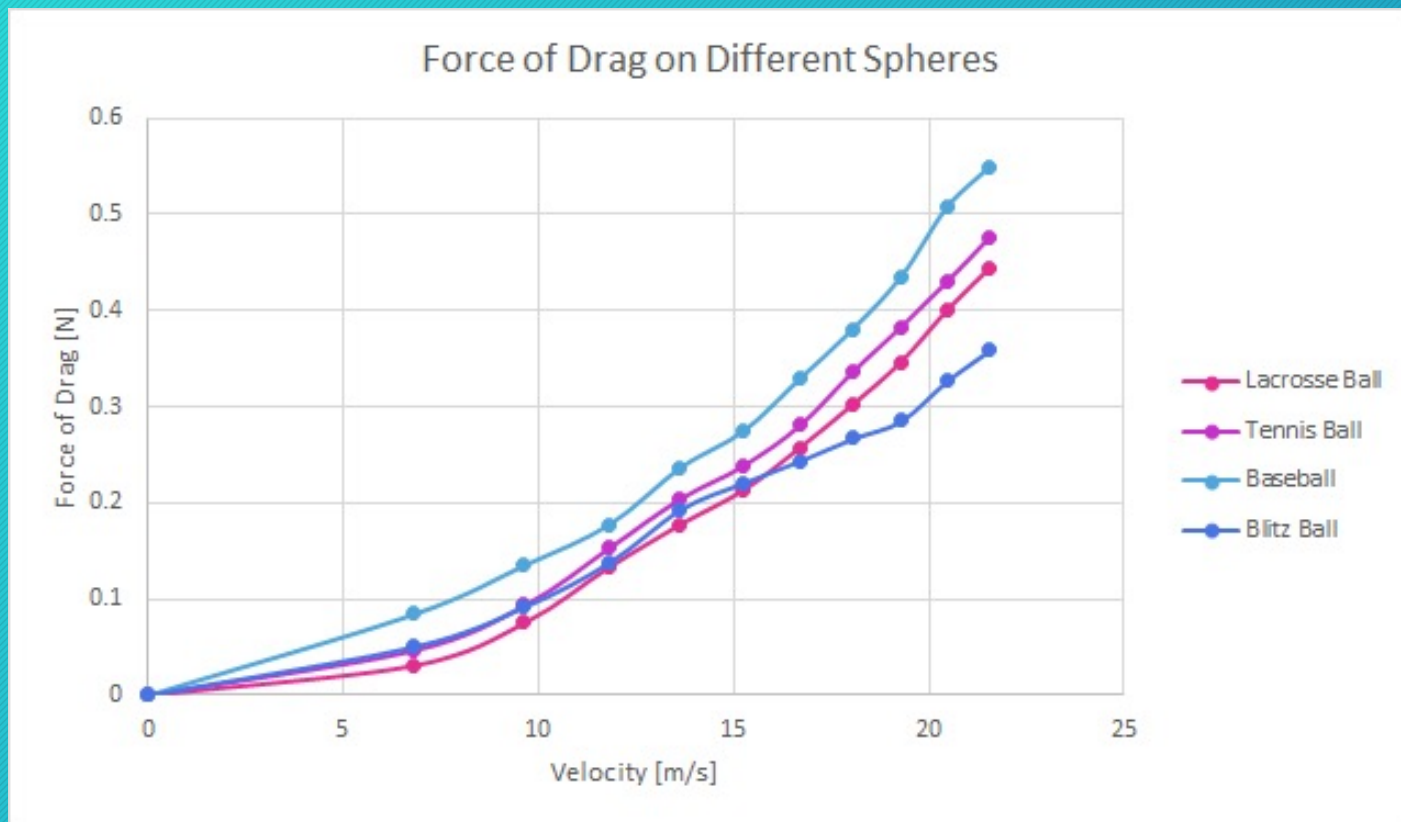
C_d = drag coefficient

A = cross-sectional area

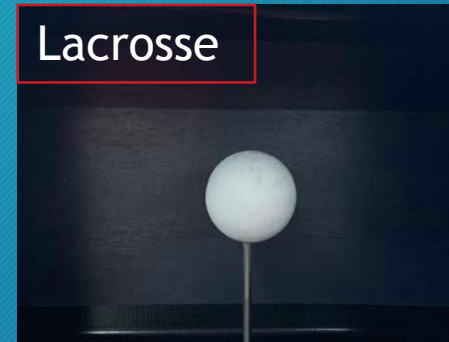


From: www.grc.nasa.gov/www/k-12/airplane/dragsphere.html

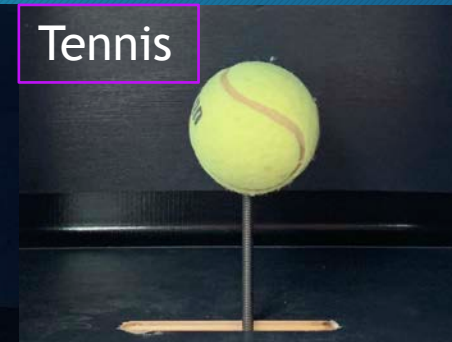
Drag forces measured at different speeds



Lacrosse



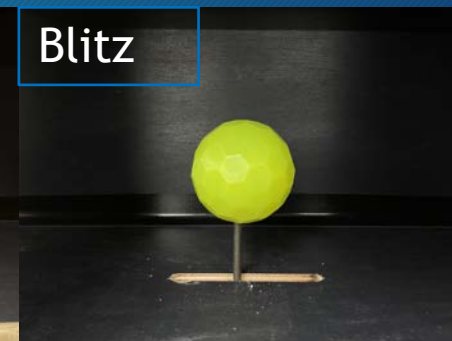
Tennis



Baseball



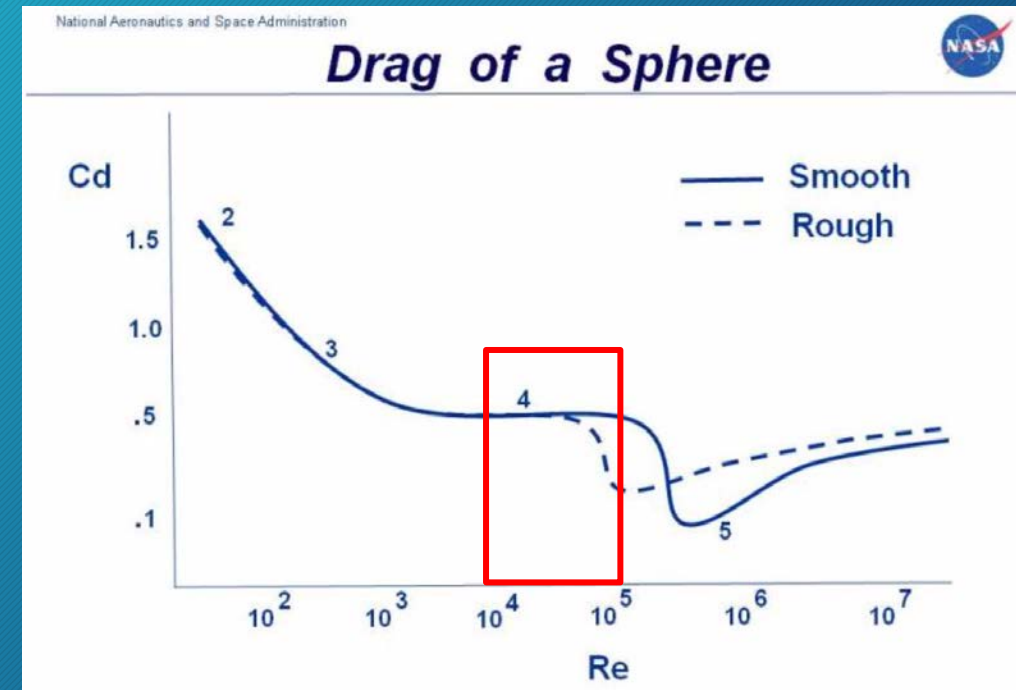
Blitz



Analysis

Spherical Object	Coefficient of Drag
Blitz ball	0.45 ± 0.06
lacrosse ball	0.49 ± 0.05
tennis ball	0.51 ± 0.02
baseball	0.64 ± 0.10

- These measurements support the idea that the shape/surface features affect the aerodynamics.
- All 4 balls behaved as expected with the coefficient of drag equal to 0.5 (within error bars).



Project 3: Drag forces on cars

Joseph (Joey) Cirillo, Cody Johnson, Demani Williams

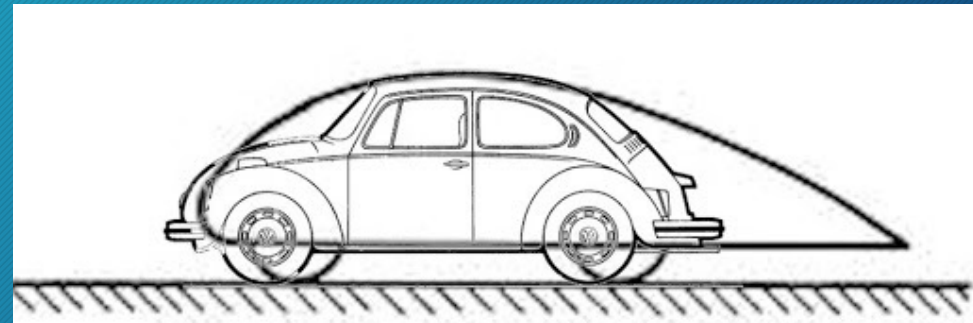
Drag can be a good thing or a bad thing, depending on the application.

- Modern efficiency vehicles: $C_d \sim 0.2$
- Volkswagen Beetle: $C_d \sim 0.5$
- Formula 1 racecar: $C_d \sim 0.7 - 1.1$



Background Information

- Most vehicles are designed to be as aerodynamic as possible
 - Lower Coefficient of Drag (C_d) requires less energy to travel through air
- Vehicles require downforce to create the appropriate normal force
 - Increase in normal force causes increased friction between tires & surface
 - Example: Formula 1, NASCAR, Sports Cars, etc... ($C_d > 0.5$)



Modeling the F1 rear wing

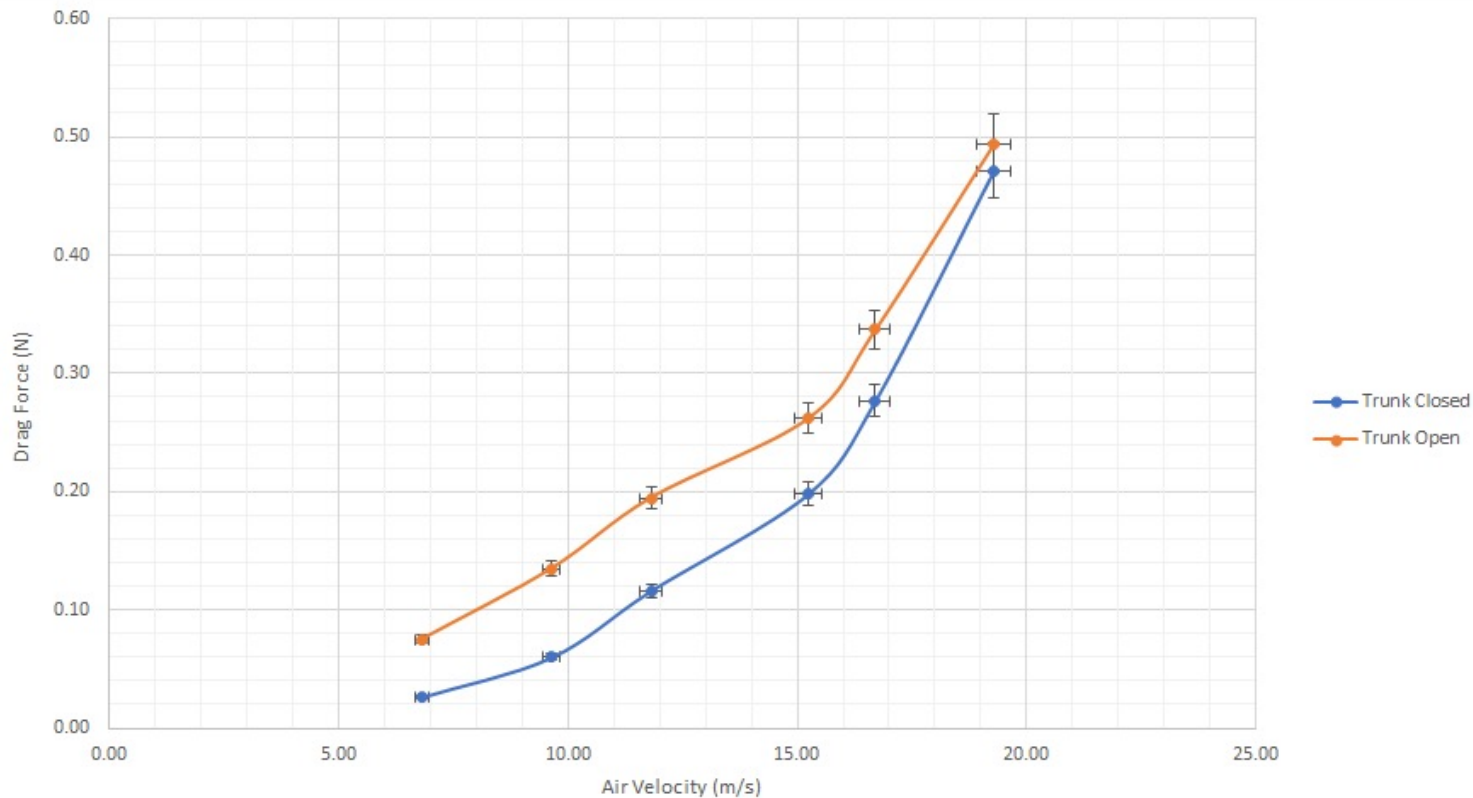
High speed (lower downforce)



High downforce (lower speed)



Drag Force vs. Air velocity of Scale VW Beetle



- Results do not exhibit a simple v^2 relationship

Drag Coefficients (C_d):

- Trunk closed = 0.26
- Trunk open = 0.40

- The trunk open C_d is larger, in agreement with expectations.

Using the measured C_d to calculate max speed

- Characteristics of a 1967 VW Beetle
 - Stock engine: 53 HP (@ 85% efficiency = 34 kW)
 - Actual size is 20x larger than scale model
 - C_d (trunk closed) = 0.26
 - C_d (trunk open) = 0.40

- $P_{\max} = (F_{\text{drag}})(v_{\max})$
 - Solving for v_{\max} →

$$v_{\max} = \sqrt[3]{\frac{\text{Power}}{\frac{1}{2} \rho_{\text{air}} C_d A}}$$

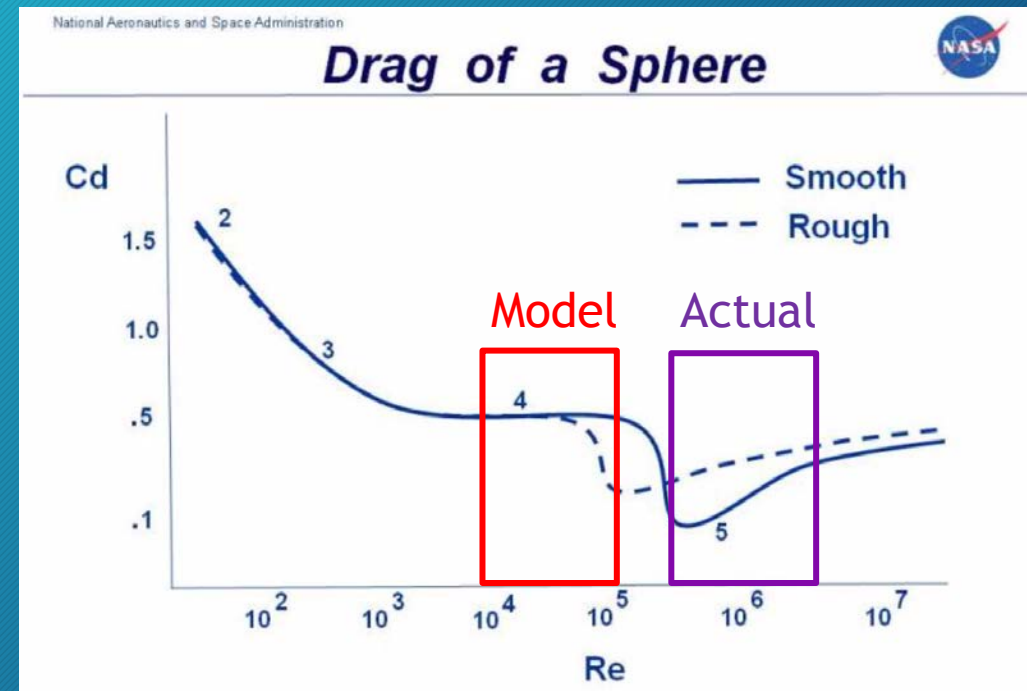
- Trunk Closed: $v_{\max} = 103$ mph
- Trunk Open: $v_{\max} = 89$ mph



Actual 67' Beetle Top Speed: 70 mph

Summary

- Calculated v_{\max} is higher than actual v_{\max}
- It is possible that the turbulent drag forces in the wind tunnel are not the same as full-scale flows.
 - $Re_{\text{model}} \sim 100,000$
 - $Re_{\text{actual}} \sim 2,000,000$

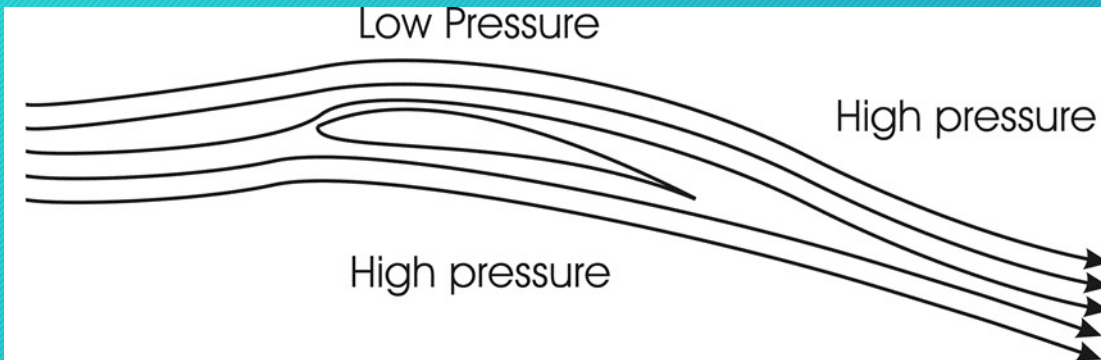


Project 4: The influence of wing shape on lift

Emily DeClerck, Zachary Fernandez

- How does wing shape affect lift?
- How does the angle of the wing affect lift?

Introduction of Wings



- Two main effects create lift in wings:
 - Lower pressure above the wing (shaping)
 - Redirection of the air flow (angle of wing)

Types of Wings

- Wing #1: flat plywood
- Wing #2: a shaped wing from a model airplane



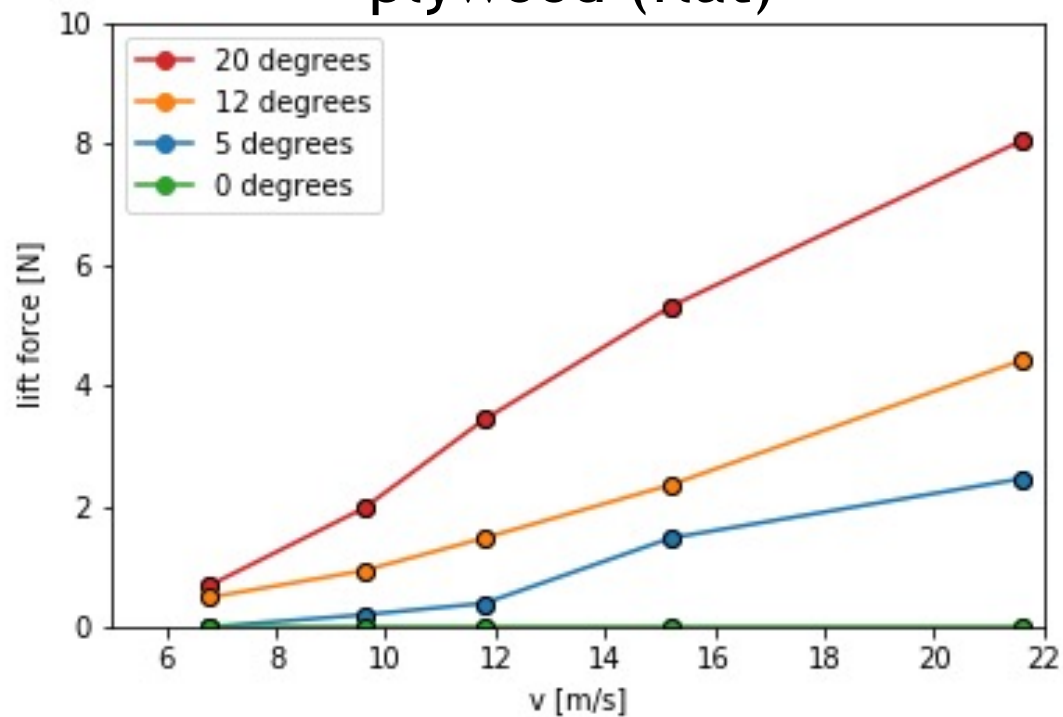
Types of Wings

- The wings have the same base area and mounting locations.



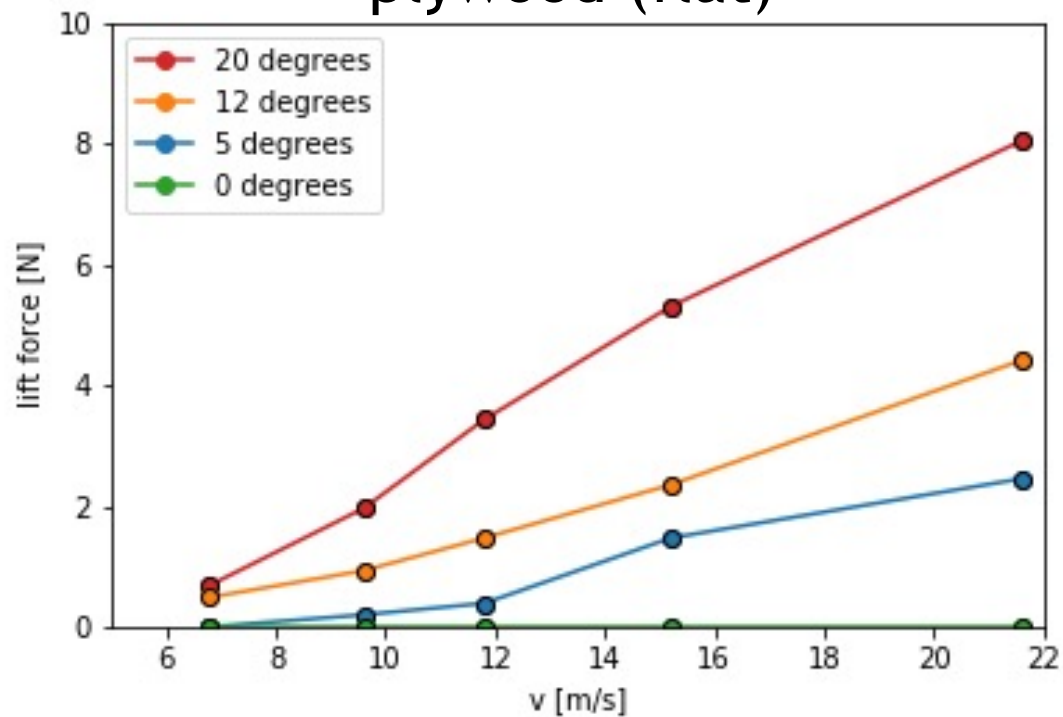
Lift increases with pitch angle (stall point not observed)

plywood (flat)

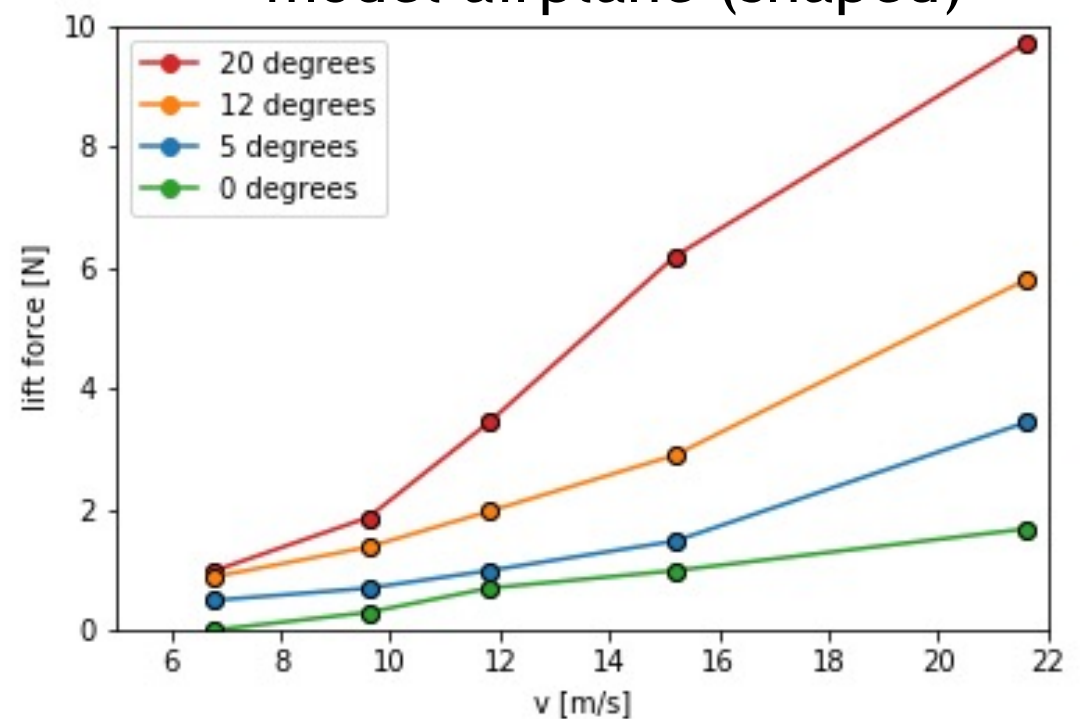


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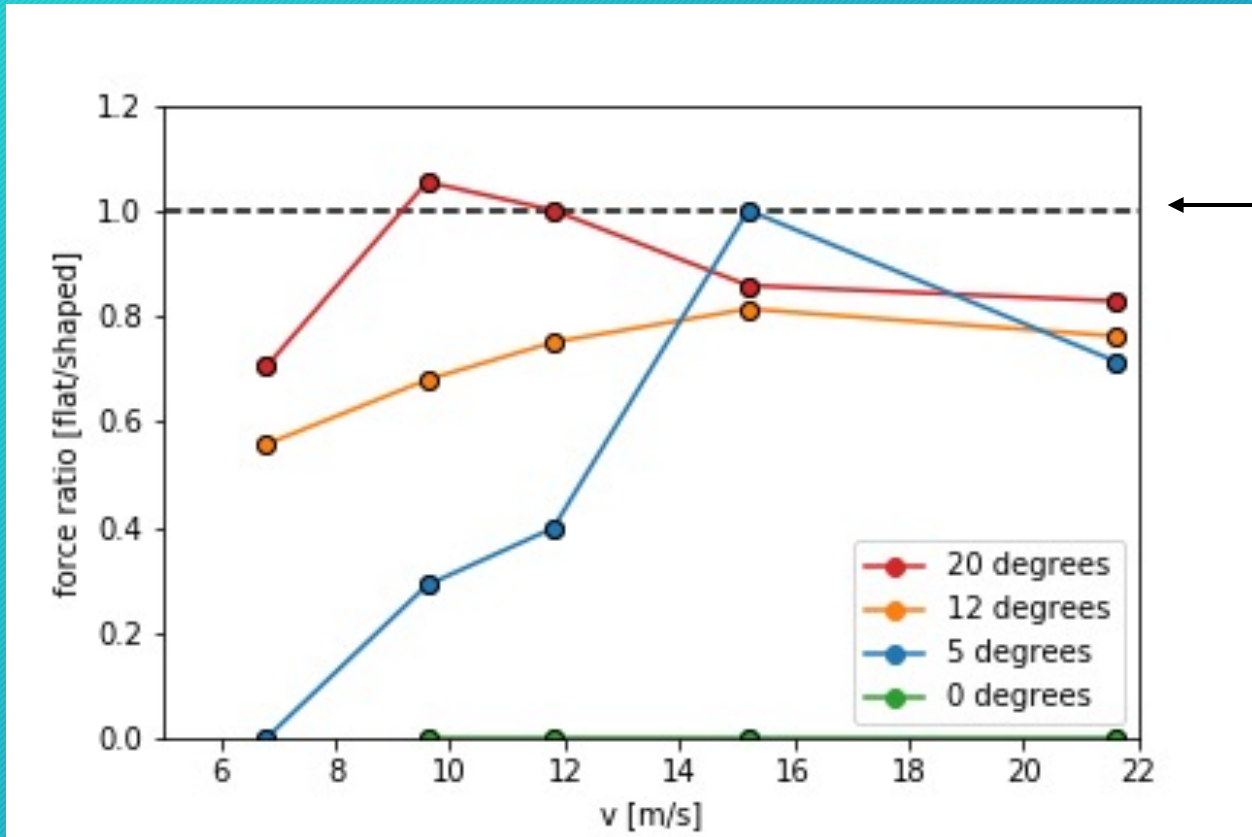
plywood (flat)



model airplane (shaped)



Pitch angle is more important than shaping at pitch angles above ~10 degrees



At a ratio of 1 the two wings behave the same

Conclusions and outlook

- Project 1: wind tunnel characterization
 - Pitot tube seems reliable, but further work needed to refine accuracy
- Project 2: drag forces on sports balls
 - Measurements strikingly close to the expected value of 0.5
 - Some tantalizing results about a ball with an unusual ball (the Baseball)
- Project 3: drag forces on vehicles
 - Seem to be measuring drag coefficients considerably lower than expected
 - This may be due to problems with extrapolation to higher Re
- Project 4: lift forces on wings
 - Lift force from shaping (pressure effect) is measurable
 - For non-zero angles of inclination the dominant effect rapidly becomes the pitch angle